



`filter_designer` – An Interactive Tool for Designing Digital Filters

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All digital filtering in Antelope utilizes **time-domain** convolution and recursive methodologies.

Digital time-domain filtering offers significant advantages over FFT based frequency-domain filtering.

1. Can operate on infinite time series in a continuous fashion.
2. Minimal edge effects that can be confined with finite time windows.
3. Much more computationally efficient.
4. Simplicity of implementation.

Implementation of Fourier transforms is done with the Discrete Fourier Transform (DFT) using a clever digital algorithm known as the Fast Fourier Transform (FFT). All DFTs, regardless of how they are implemented, are necessarily computed over finite time windows, usually no more than thousands of time samples, which cause them to be subject to an artifact known as “wraparound”.

FFT computational efficiency of order $5 * N * \log_2(N)$
brute force direct time-domain convolution computational efficiency of order $2 * N * N$.

However, most convolutions involve one function (the filter impulse response) with a reduced and constant value of N .

All filtering of time sampled waveforms in Antelope are done in the time domain and do not involve the computations of signal spectra using FFTs.

All Antelope digital time domain filters can be applied to arbitrary time series and can be applied to continuous time series of indefinite length.

There are no inherent time windowing parameters needed by the Antelope filters as there would be if filtering were done in the frequency domain. No “wraparound” effects.

The Antelope time domain filters are very computationally efficient compared to frequency domain methods

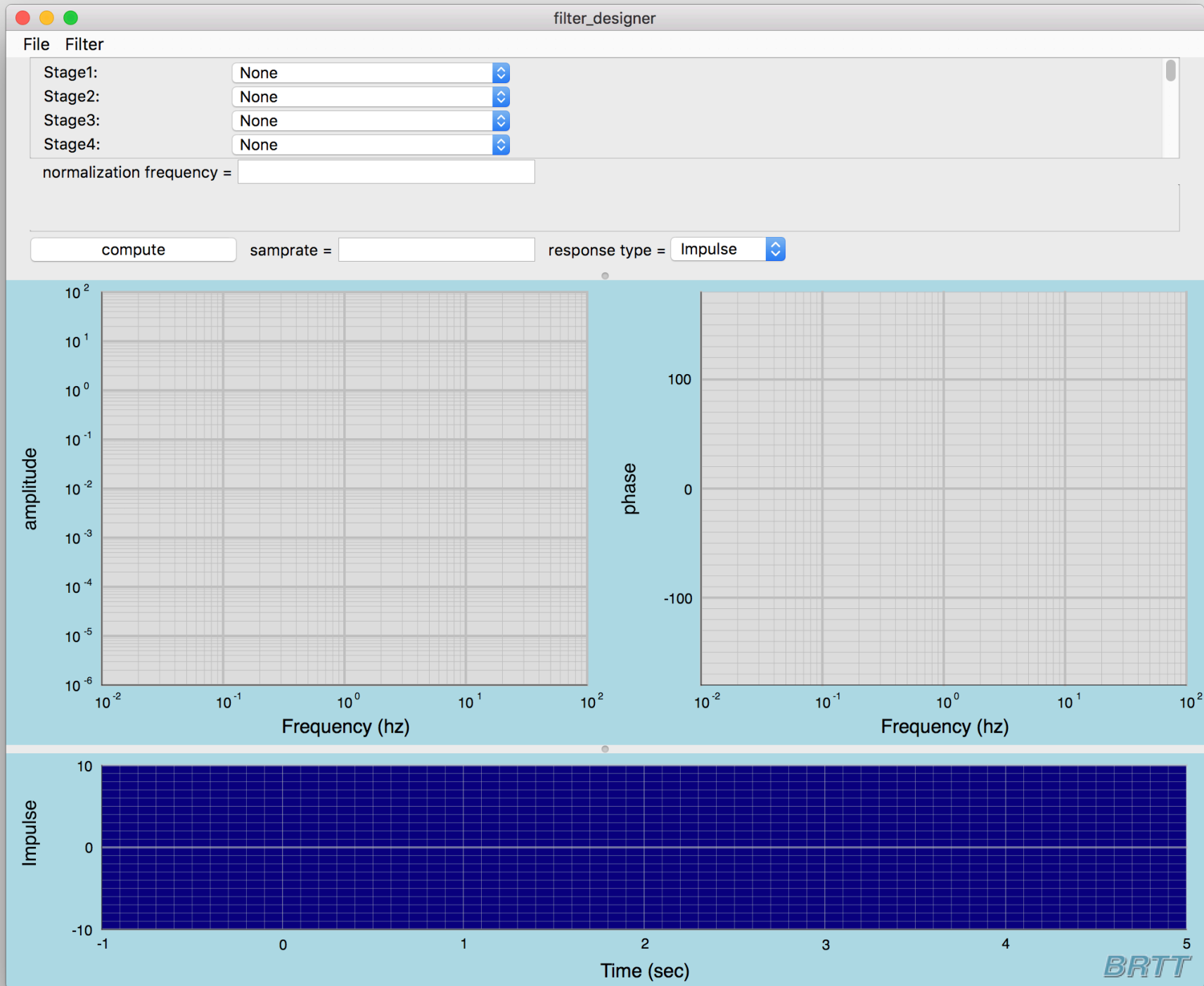
All Antelope time domain filters are implemented with the **wffil(3)** library which provides general purpose interfaces to various time domain waveform filter methods.

Specific filtering groups are defined in **wffilbrtt(3)**, which includes Butterworth, generalized S-domain polynomials, differentiator, integrator, Wood-Anderson instrument response, generalized FIR filters, and **wffilave(3)**, which provides a variety of averaging filters.

Most filtering in Antelope for the purpose of data processing, such as the filters used in **orbdetect** for example, is done using recursive digital filters also known as Infinite Impulse Response, or IIR, filters.

A new application, **filter_designer**, is available in the 5.8 release of Antelope. This app provides the design and visualization of Antelope IIR filters.

Python script using the new Antelope `pythonbqplot` (3Y) python graphics libraries



Stage1:

Stage2:

Stage3:

Stage4:

normalization frequency =

compute

response type =

- ✓ None
- 1st order low pass
- 1st order high pass
- 2nd order low pass
- 2nd order high pass
- Inverted 1st order low pass
- Inverted 1st order high pass
- Inverted 2nd order low pass
- Inverted 2nd order high pass
- Butterworth
- Wood-Anderson displacement
- Wood-Anderson velocity
- Wood-Anderson acceleration
- Integrate Once**
- Integrate Twice
- Differentiate Once
- Differentiate Twice

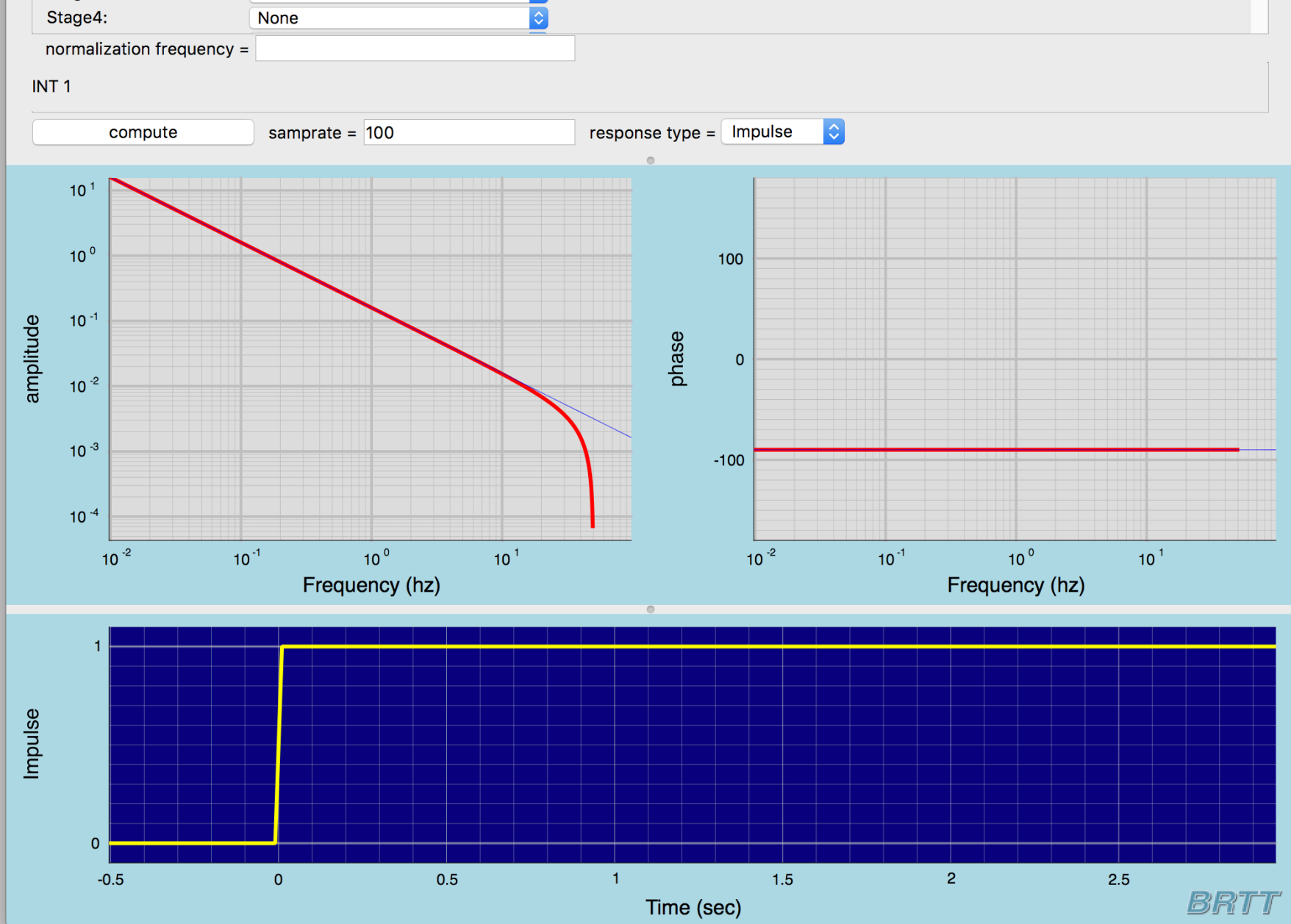
amplitude

10^2
 10^1
 10^0
 10^{-1}
 10^{-2}
 10^{-3}
 10^{-4}

phase

Type	S-domain transfer function	Antelope filter string	Description
1st order low pass		DF C	first order denominator polynomial suitable as a zero frequency normalized first order low-pass filter
1st order high pass		DFDIF1 C	first order denominator polynomial with a single differentiation suitable as an infinite frequency normalized first order high-pass filter
2nd order low pass		DS B C	second order denominator polynomial suitable as a zero frequency normalized second order low-pass filter
2nd order high pass		DSDIF2 B C	second order denominator polynomial with a double differentiation suitable as an infinite frequency normalized second order high-pass filter

Filter stages are defined in **wffilbrtt(3)**



The red line is the digital Z-domain response. The thin blue line is the analog response. Note the effects of the frequency warping.

Stage3: None

Stage4: None

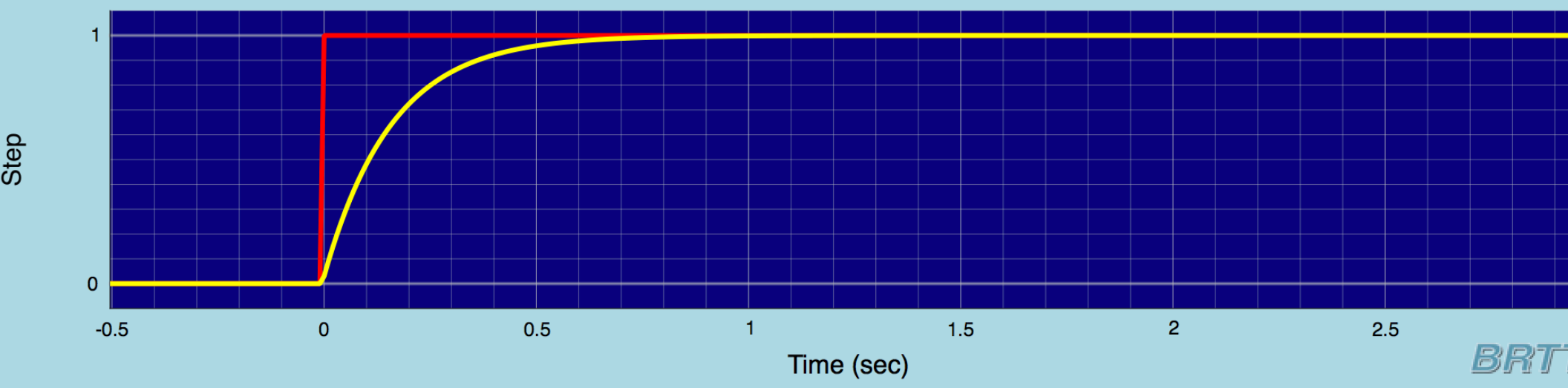
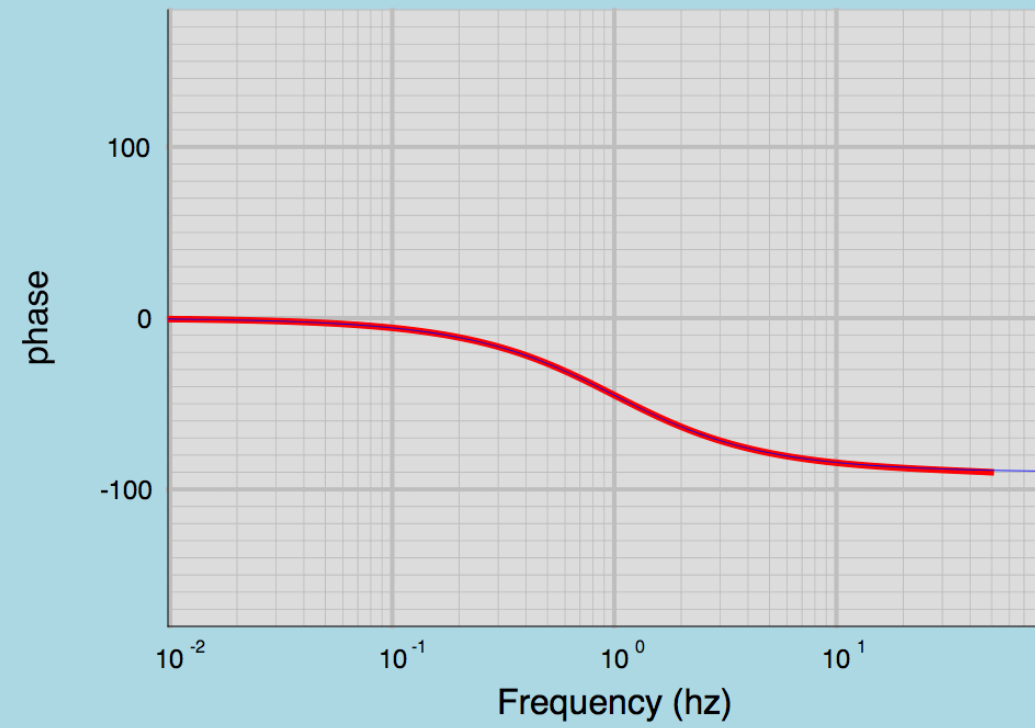
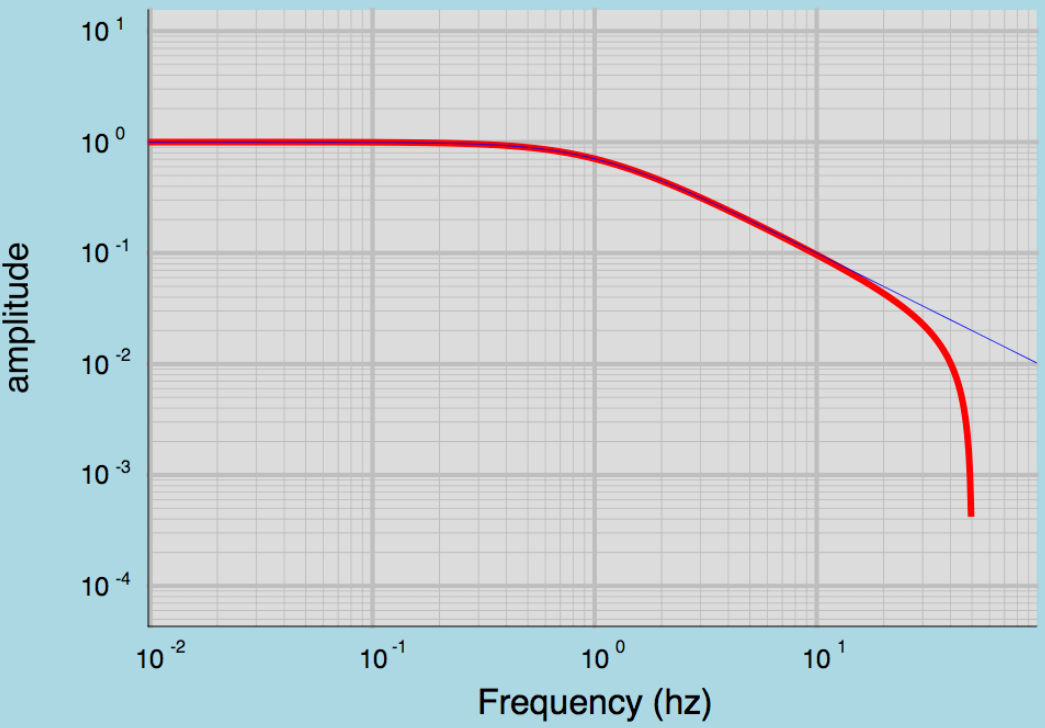
normalization frequency =

SPF DF 6.283185e+00

compute

samprate = 100

response type = Step



Stage3: None

Stage4: None

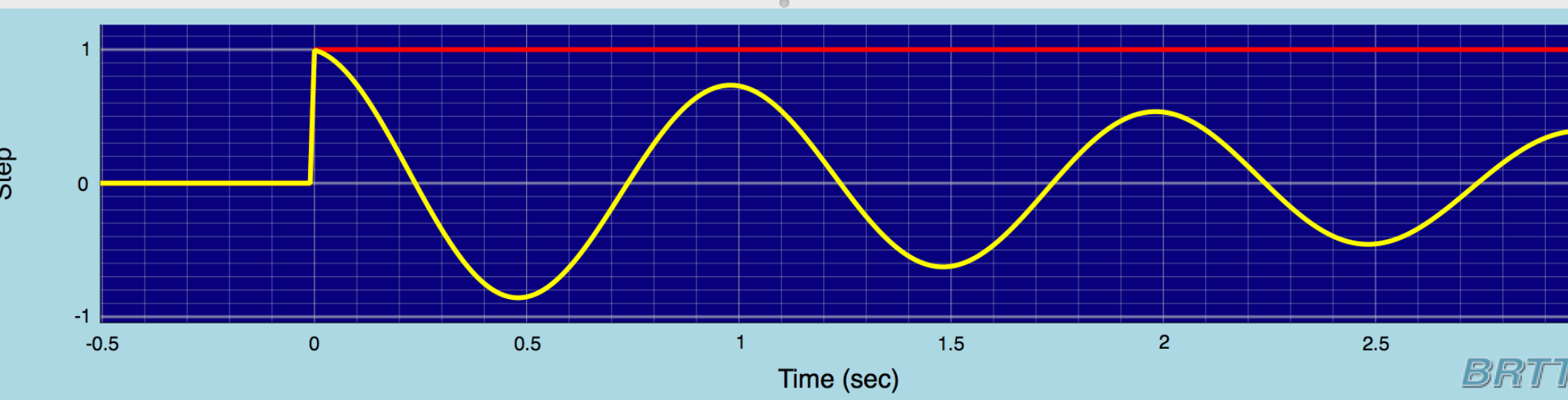
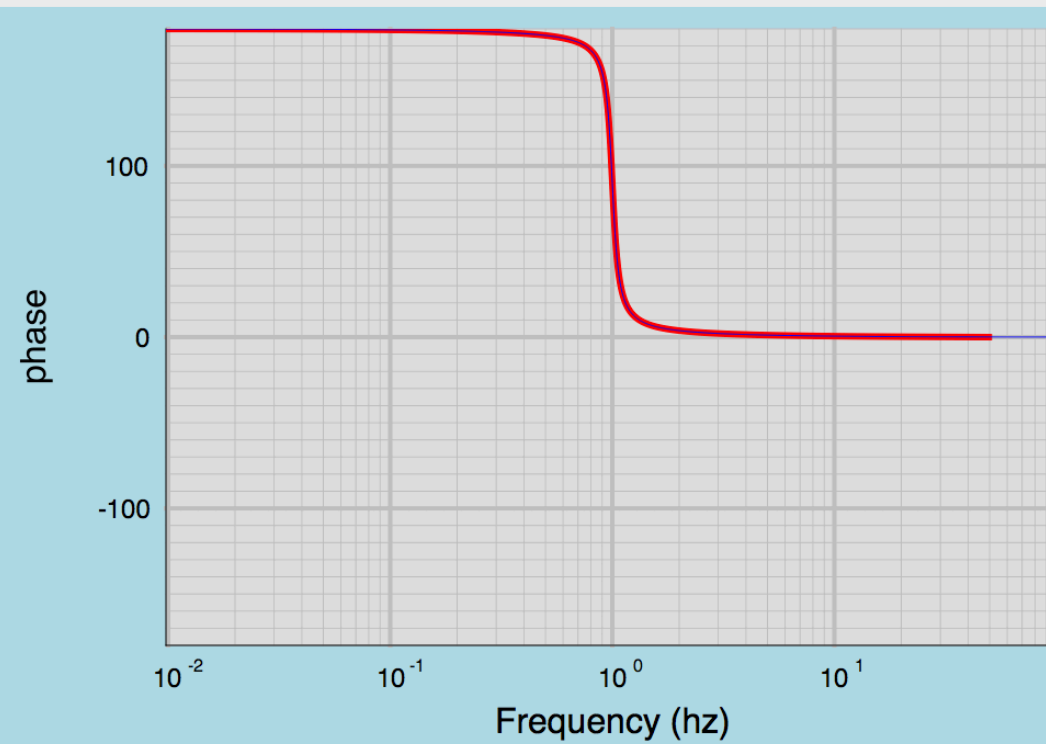
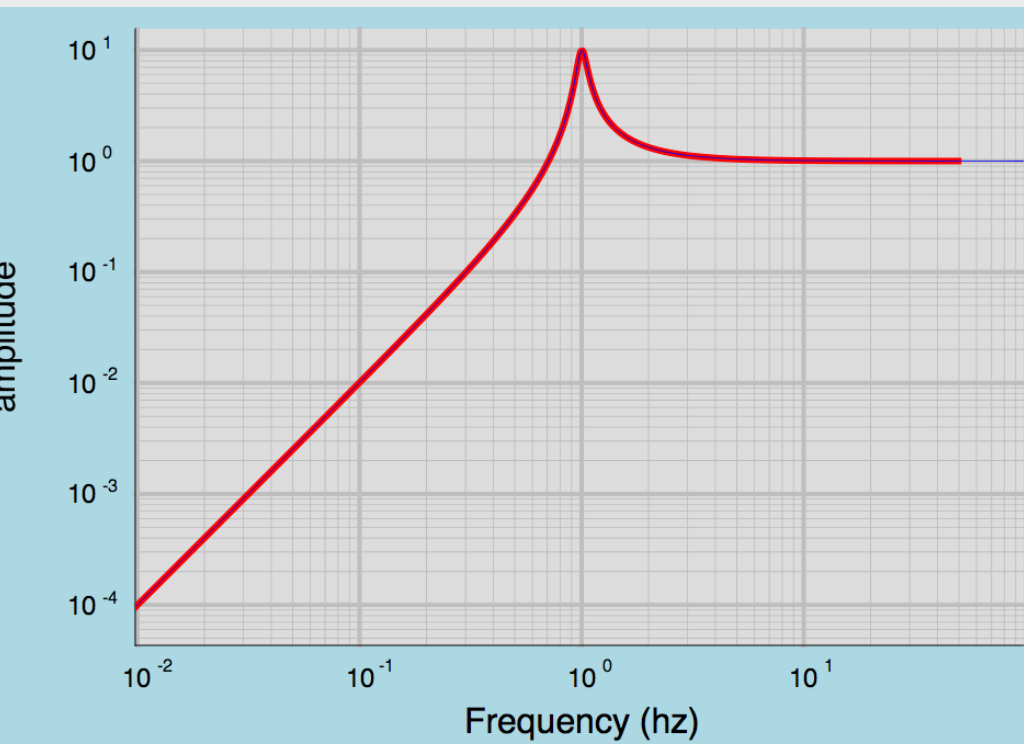
normalization frequency =

SPF DSDIF2 6.283185e-01 3.947842e+01

compute

samprate = 100

response type = Step



Stage3: None

Stage4: None

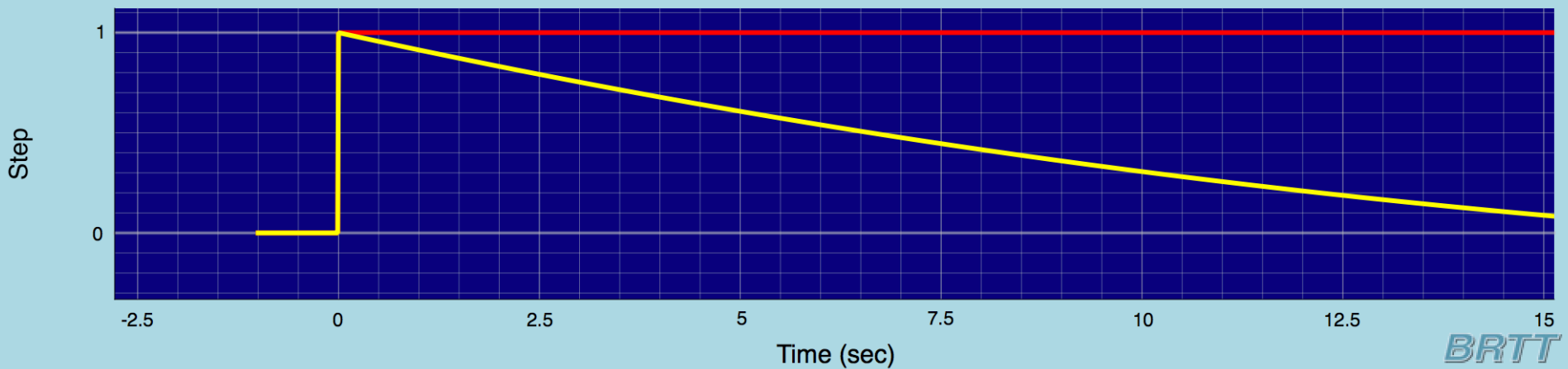
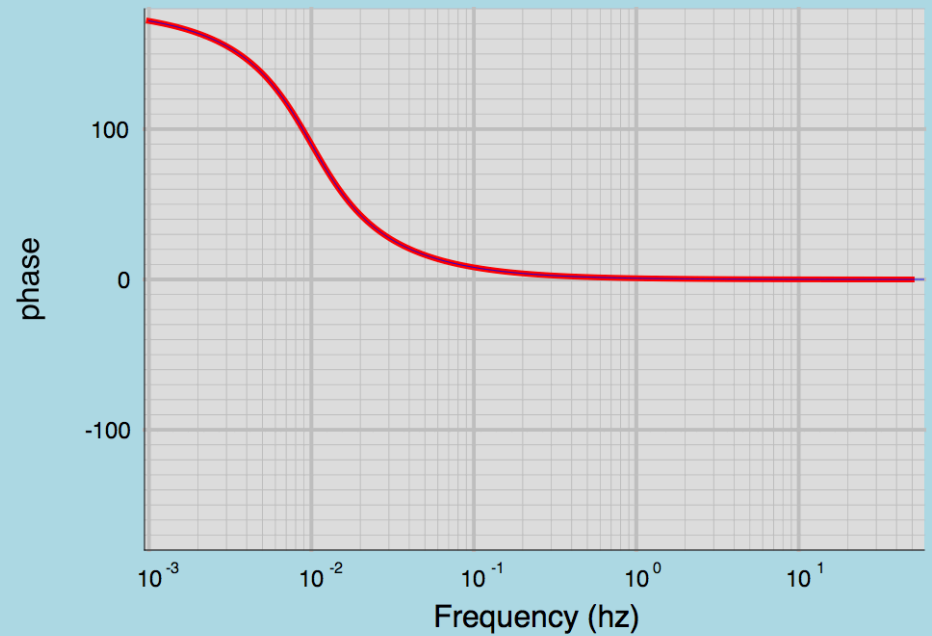
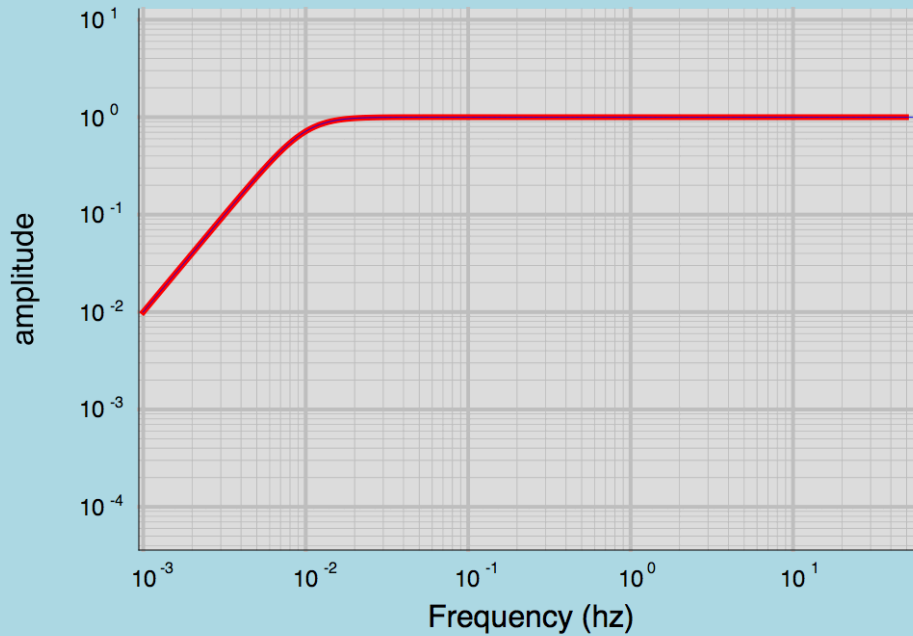
normalization frequency =

SPF DSDIF2 8.796459e-02 3.947842e-03

compute

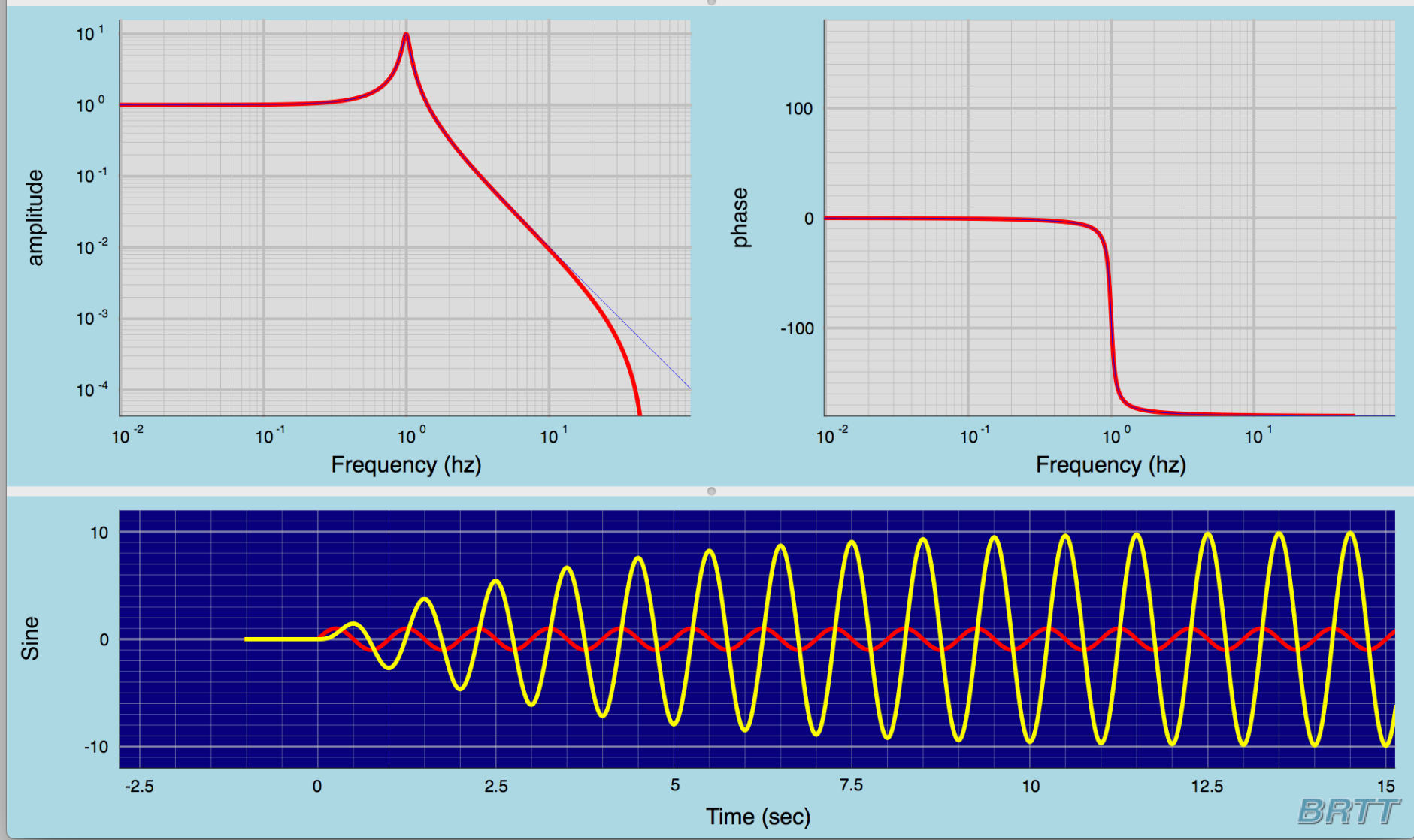
samprate = 100

response type = Step



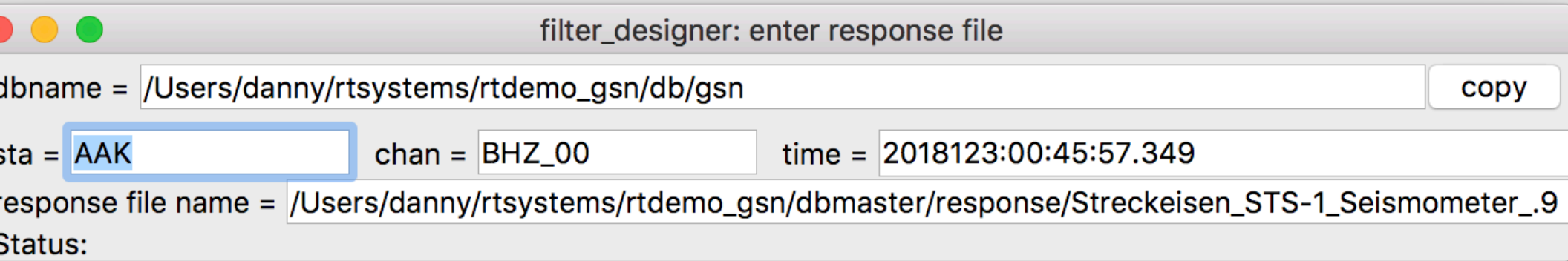
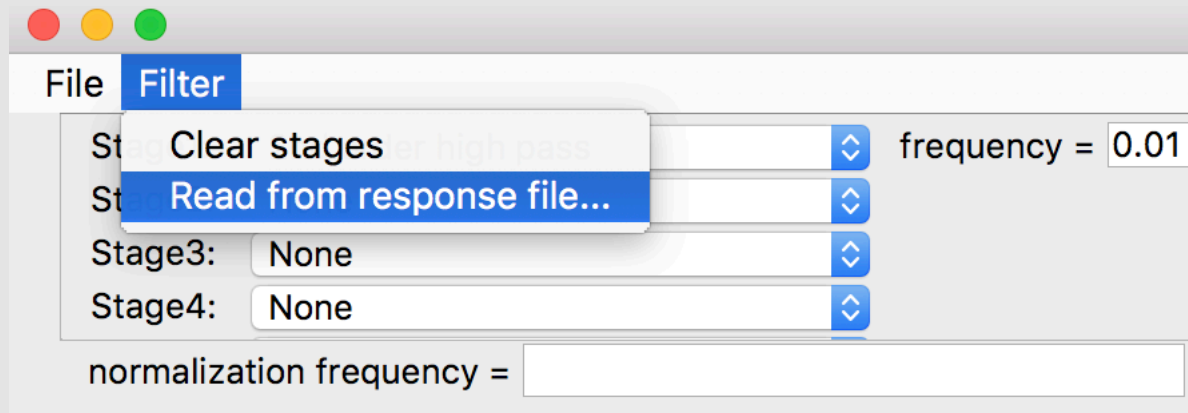
Basic seismometer response (note the filter string

Stage2:
Stage3:
Stage4:
normalization frequency =
SPF DS 6.283185e-01 3.947842e+01
 samprate = response type = frequency =



Strong motion response function.

Grab real instrument responses



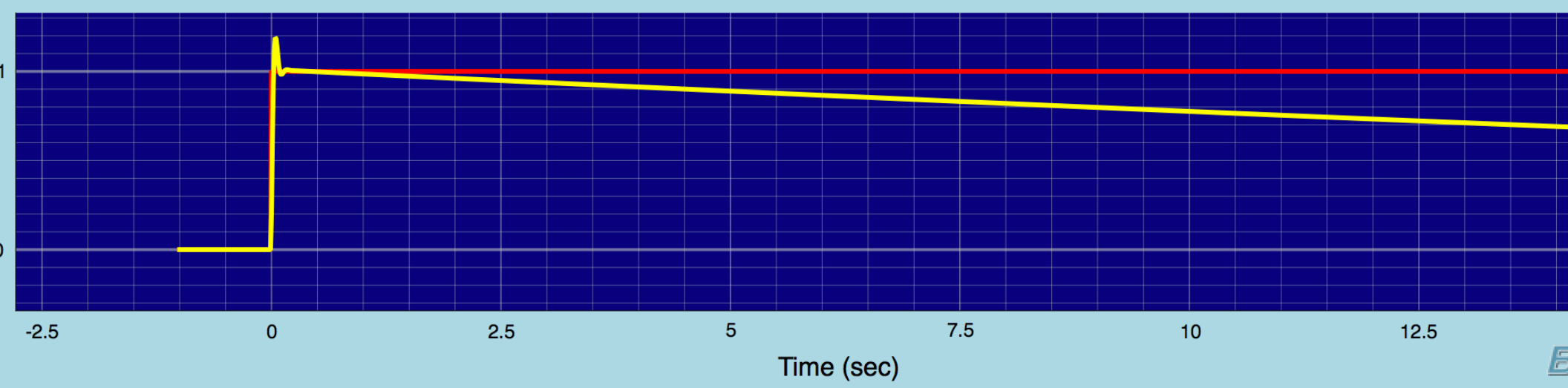
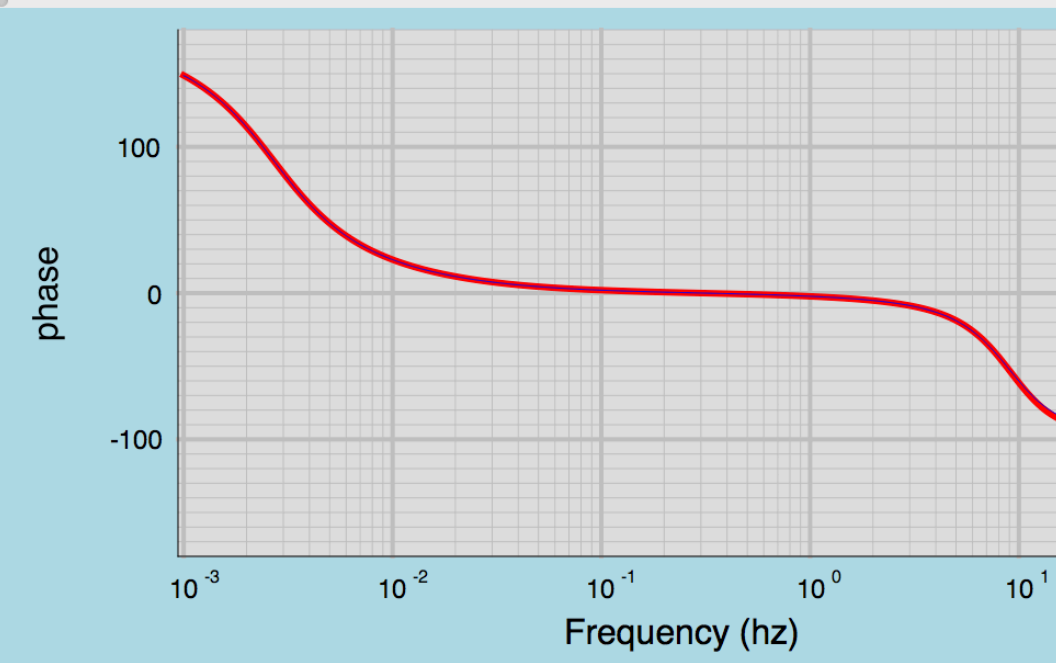
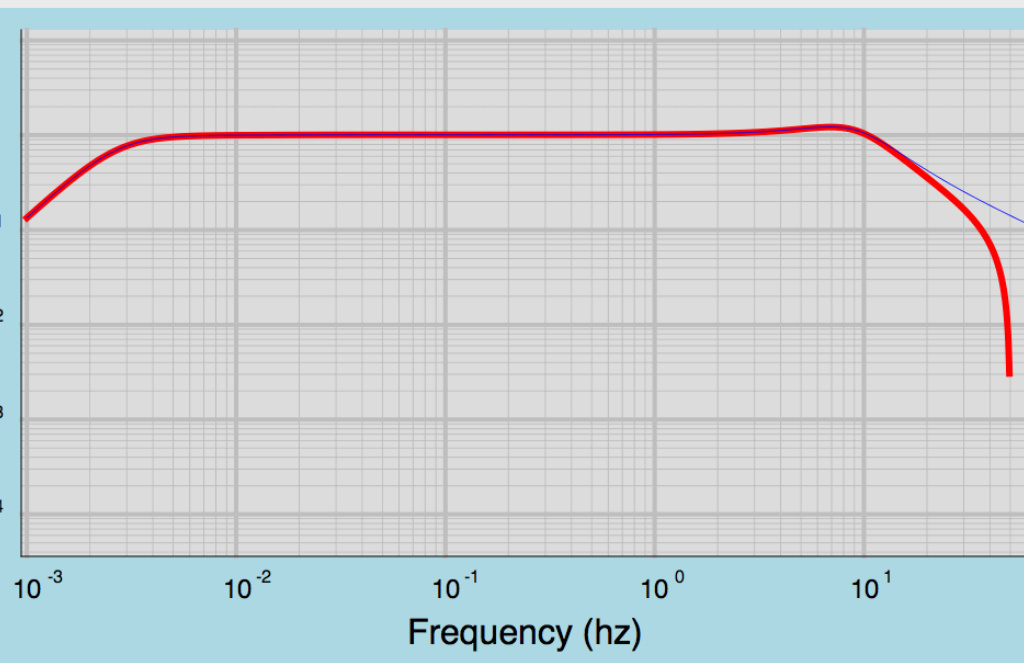
- 3: Inverted 1st order low pass frequency = 0.0242718000002
- 4: 2nd order low pass frequency = 0.0243926703301
- 5: 2nd order low pass frequency = 9.17499977475
- 6: Inverted 1st order low pass frequency = 12.5

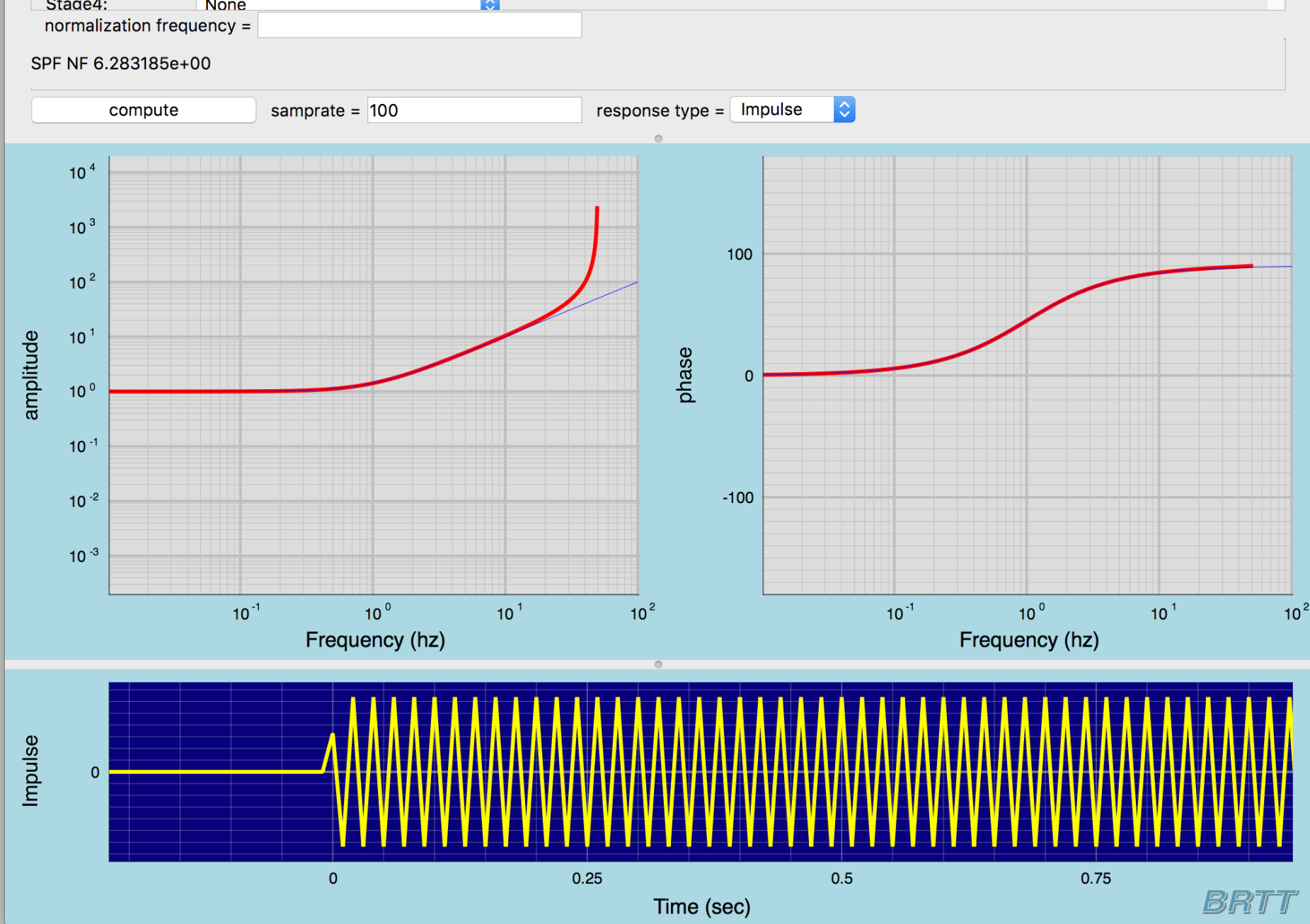
damping = 0.996000014423
 damping = 0.55499946866

Normalization frequency =

DIF2 2.423538e-02 2.904693e-04 , NF 1.525042e-01 , NF 1.525042e-01 , DS 3.053012e-01 2.348975e-02 , DS 6.398947e+01 3.323318e+03 , NF 7.853982e

compute samprate = 100 response type = Step





verted filter stages are inherently unstable. They should
be used in combination with non-inverted filter stages

