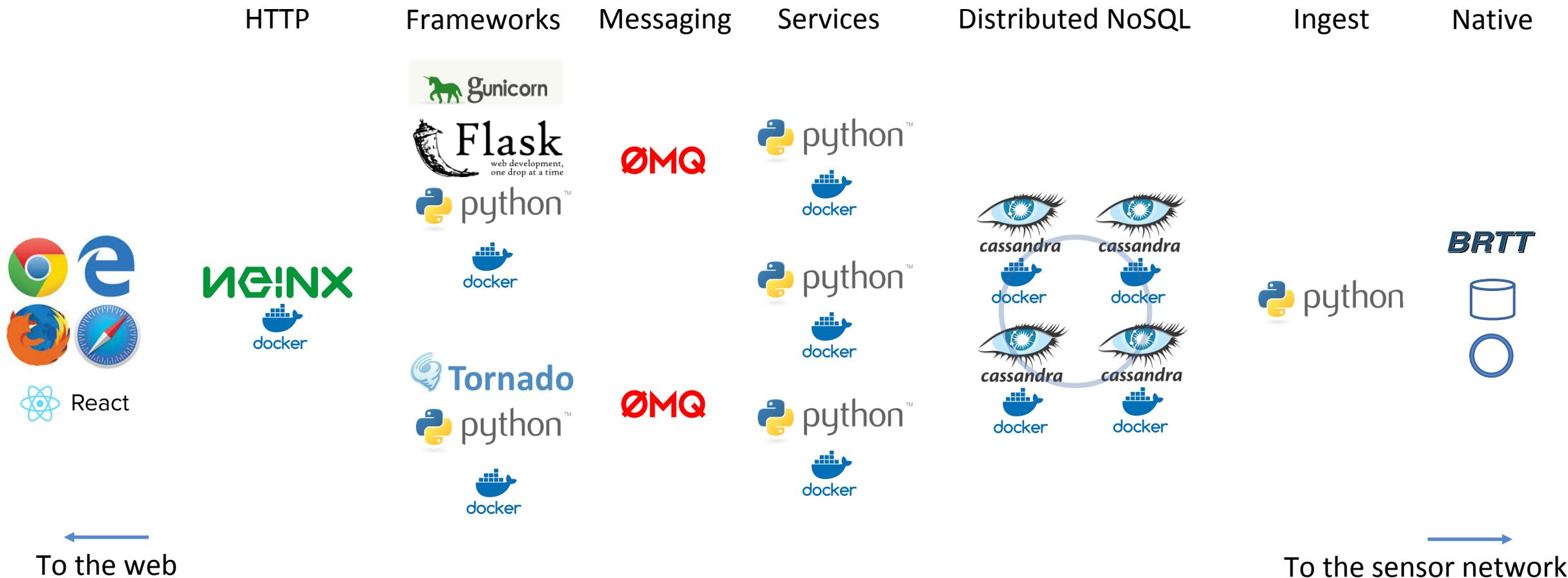
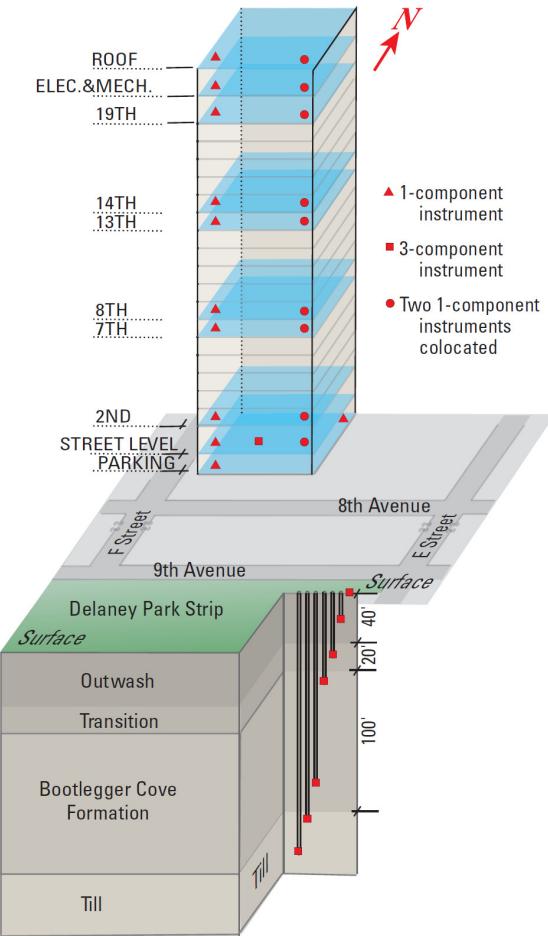


What is a Sensible Architecture for an Antelope-Powered Web Service?

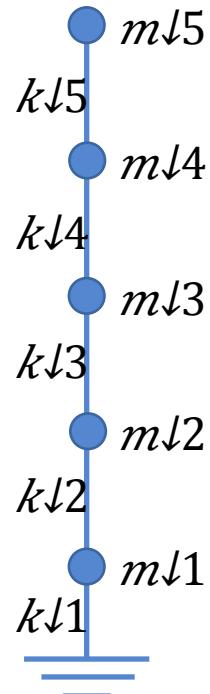


Structural Health Monitoring

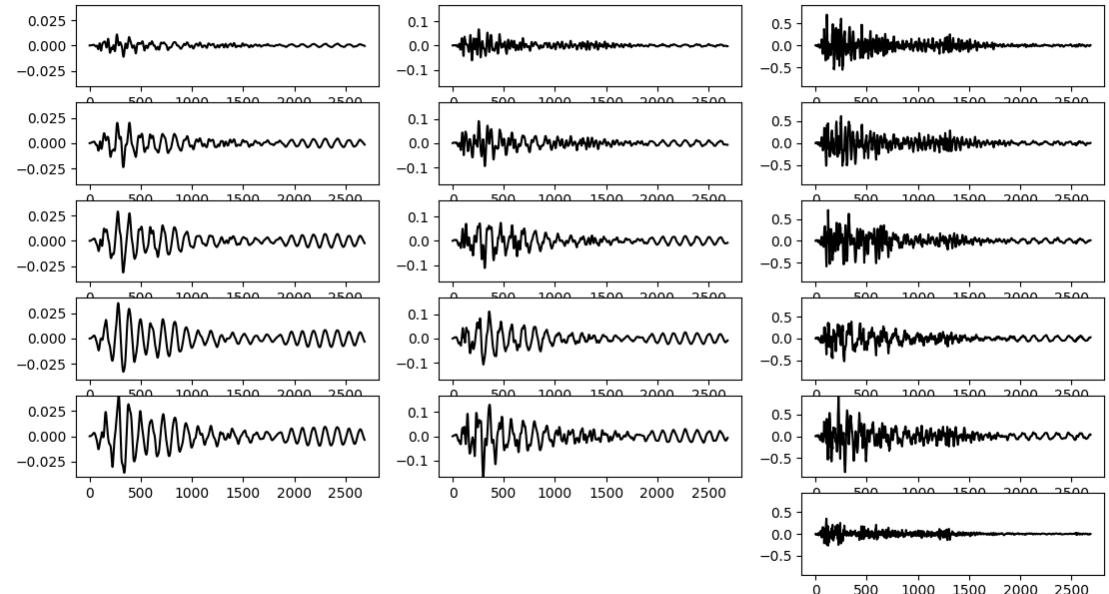
Instrumentation



Model

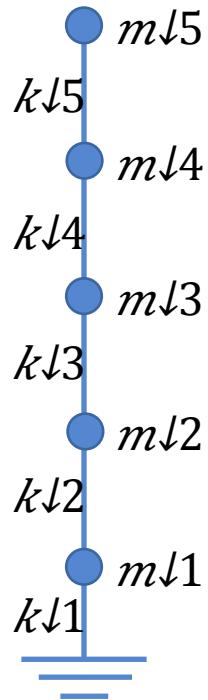


Signal



Atwood Building, Anchorage
UCSB Geotechnical Array monitoring program

Equations of Motion and Objective Function



$$Mu(t) + Cu(t) + Ku(t) = -Mrg(t)$$

Put into state space form
Discretize

$$x(k+1) = Ax(k) + Bg(k)$$

$$y(k) = Cx(k) + Dg(k)$$

Unwind recursions

$$x(k) = \sum_{l=1}^{k-1} A^{k-l-1} B g(k-l)$$

$$y(k) = \sum_{l=1}^{k-1} A^{k-l-1} C B g(k-l) + D g(k)$$

Objective: sum of squares of acceleration residuals at all DOFs

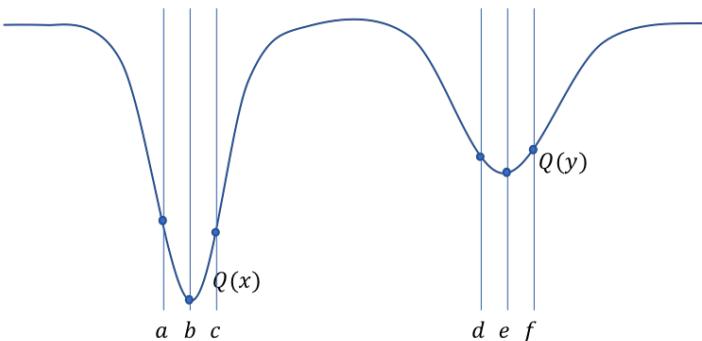
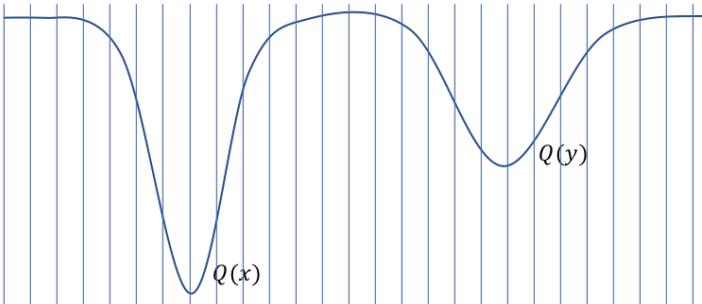
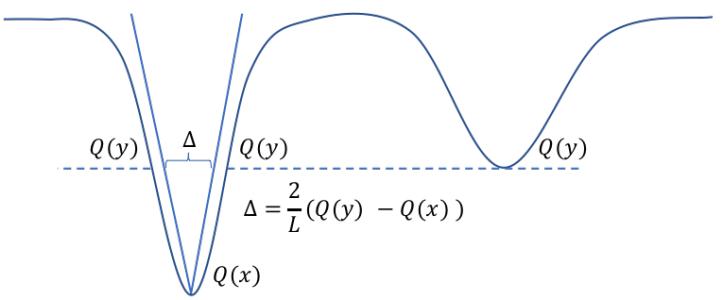
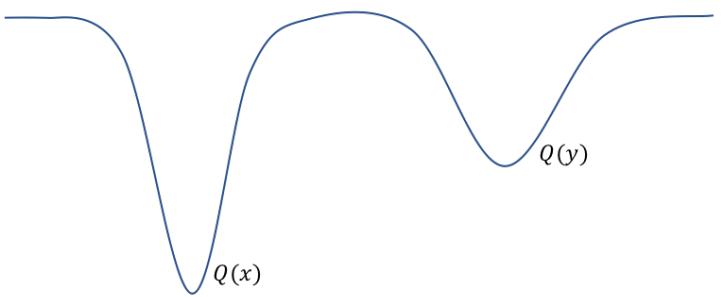
$$x^{\dagger*} = \{M^{\dagger*}, K^{\dagger*}, C^{\dagger*}\} = \arg \min \frac{1}{2} \|f(x)\|_2^2$$

$$= \arg \min \frac{1}{2} \sum_{k=0}^{T-1} \sum_{i=1}^{n_d} f_{\downarrow i}(x, k)^2$$

$$f_{\downarrow i}(x, k) = y_{\downarrow i}(x, k) - u_{\downarrow i}(k)$$

Model for accelerations in unknown physical parameters

Black Box Optimization



Randomized Black Box Coordinate Search

```

k=0
while not terminate:
    for i=shuffle(1...n):
        [a,c] = bracket_min(xi)
        xi = arg min Q(xi)
    end for
    k=k+1
end while
return x

```

↑
1-D Golden Section Search

Simulation Procedure

Choose parameters

Continuous time State space

Discrete time State space

Recursions

Acceleration model

$$x = \{M, K, C\}$$



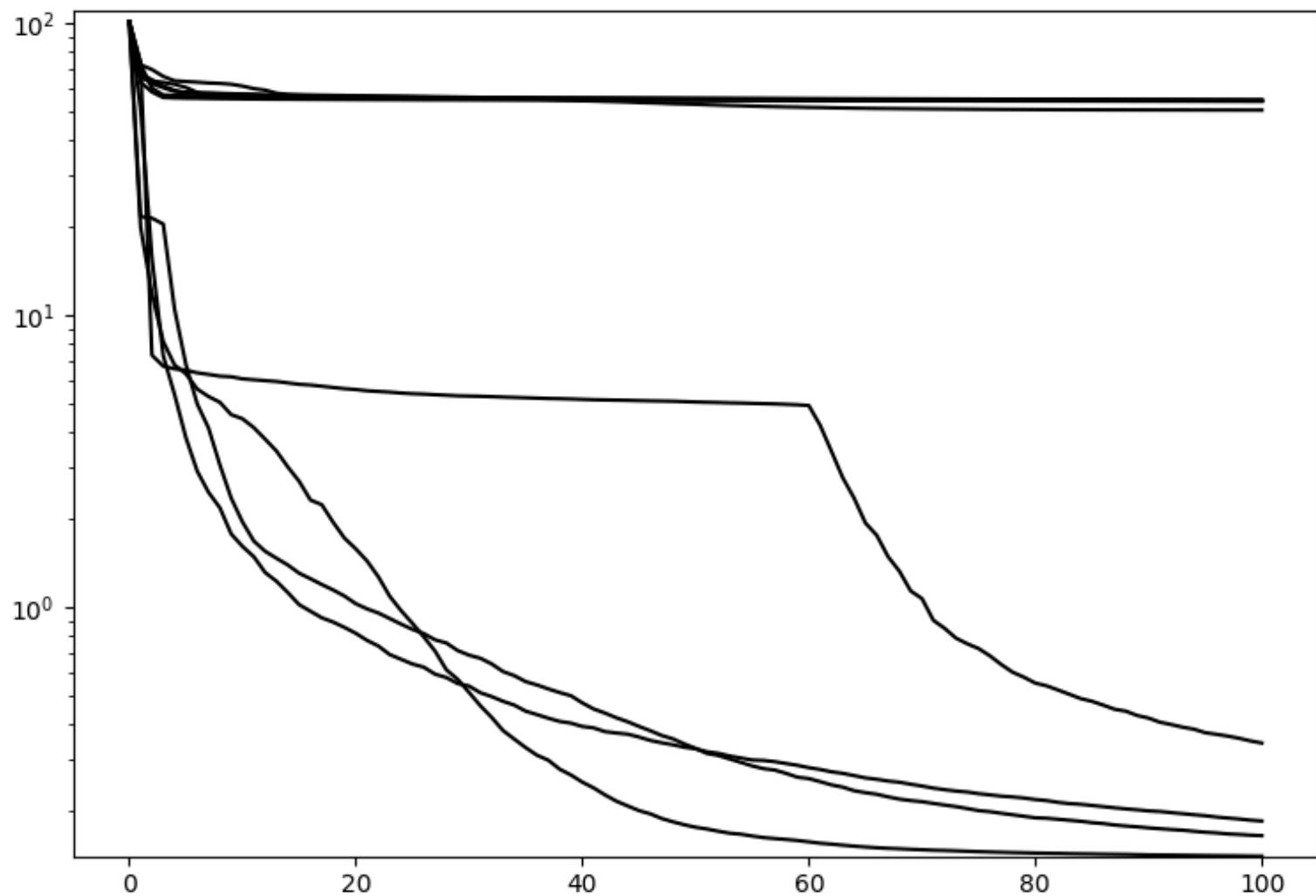
$$A \downarrow c, B \downarrow c, C, D$$

$$A, B, C, D$$



$$y(k) = \sum_{l=1}^k CA^{\uparrow l-1} B g(k-l) + D g(k)$$

Performance of Solutions over Multiple Runs



The approach works well, but can be slow. Can we improve efficiency? Yes:

- GPU versions of random coordinate search?
- Improved algorithms based on local models*

$$Q(x) \approx Q(x) = a \downarrow 0 + a \uparrow T x + 1/2 x \uparrow T H x$$

Local quadratic model
at iteration k

$$Q(x \downarrow i) = Q(x \downarrow i) \quad \forall x \downarrow i \in X$$

Interpolate against
nearby simulations
to find model
(linear system,
simplex or random)

$$x \downarrow k+1 = \arg \min Q(x \downarrow k) \quad \text{Minimize model}$$

$$C(x \downarrow k+1) = (x \downarrow k+1 - x \downarrow k) \uparrow T (x \downarrow k+1 - x \downarrow k) - \Delta^2 = 0$$

at distance Δ from
current iterate

Lagrange multipliers gives a solution

$$x \downarrow k+1 = - \sum_{i=1}^n (u \downarrow i \uparrow T \nabla Q(x \downarrow k) / \lambda \downarrow i - \lambda) v$$

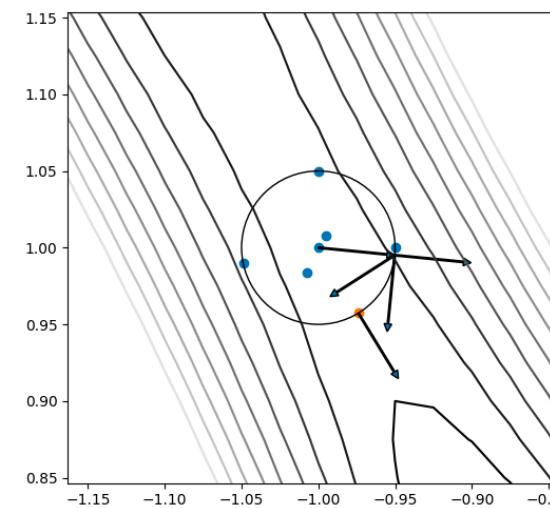
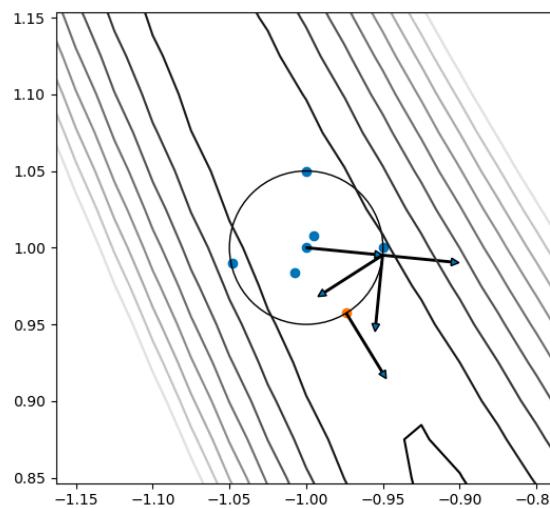
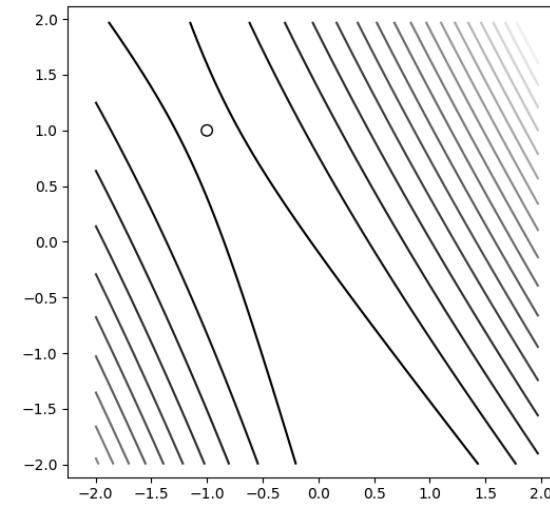
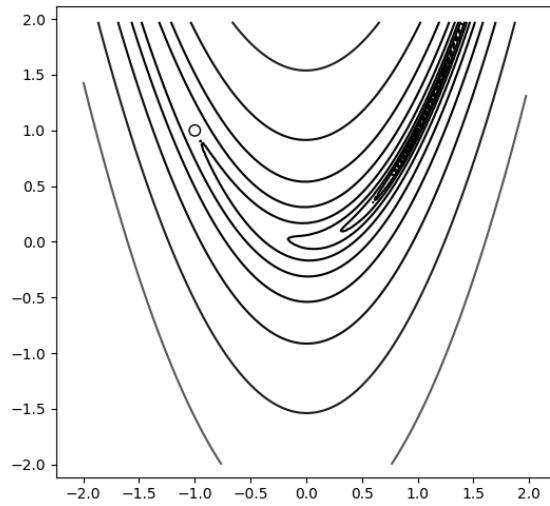
with Eigendecomposition $H = U \Lambda U \uparrow T$

$$\sum_{i=1}^n (u \downarrow i \uparrow T \nabla Q(x \downarrow k) / \lambda \downarrow i - \lambda) v$$

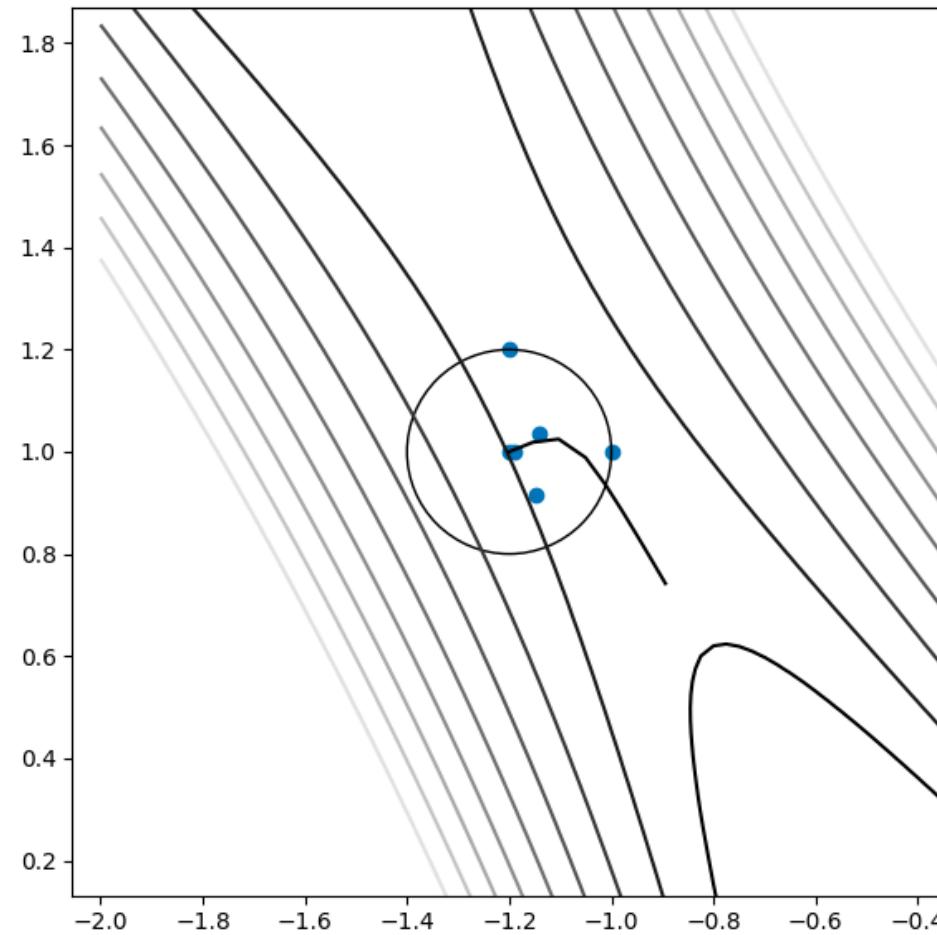
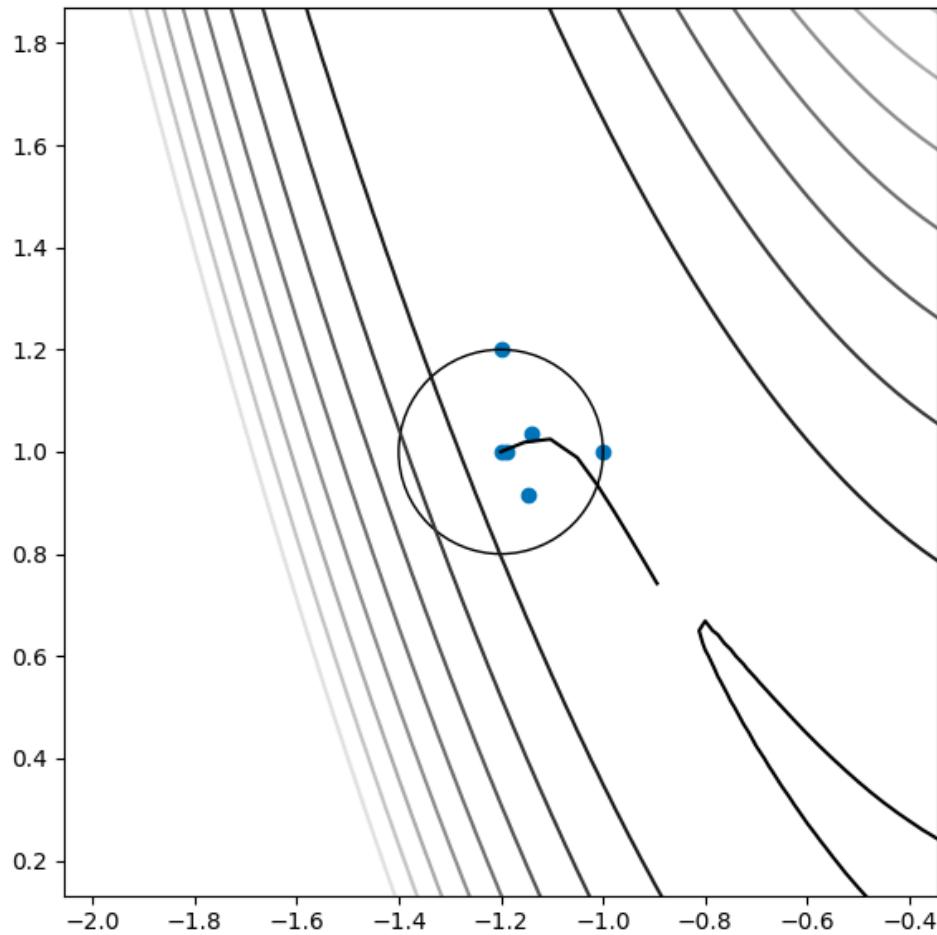
and λ given by

- A different solution direction arises as we grow Δ .
- This is a 1-D nonlinear search direction.
- Apply grid search and golden section search as before on this nonlinear direction.
- Only searching in 1 NL dimension instead of n.
- Using local info produces good descent.
- ~100x faster.
- Provably convergent.

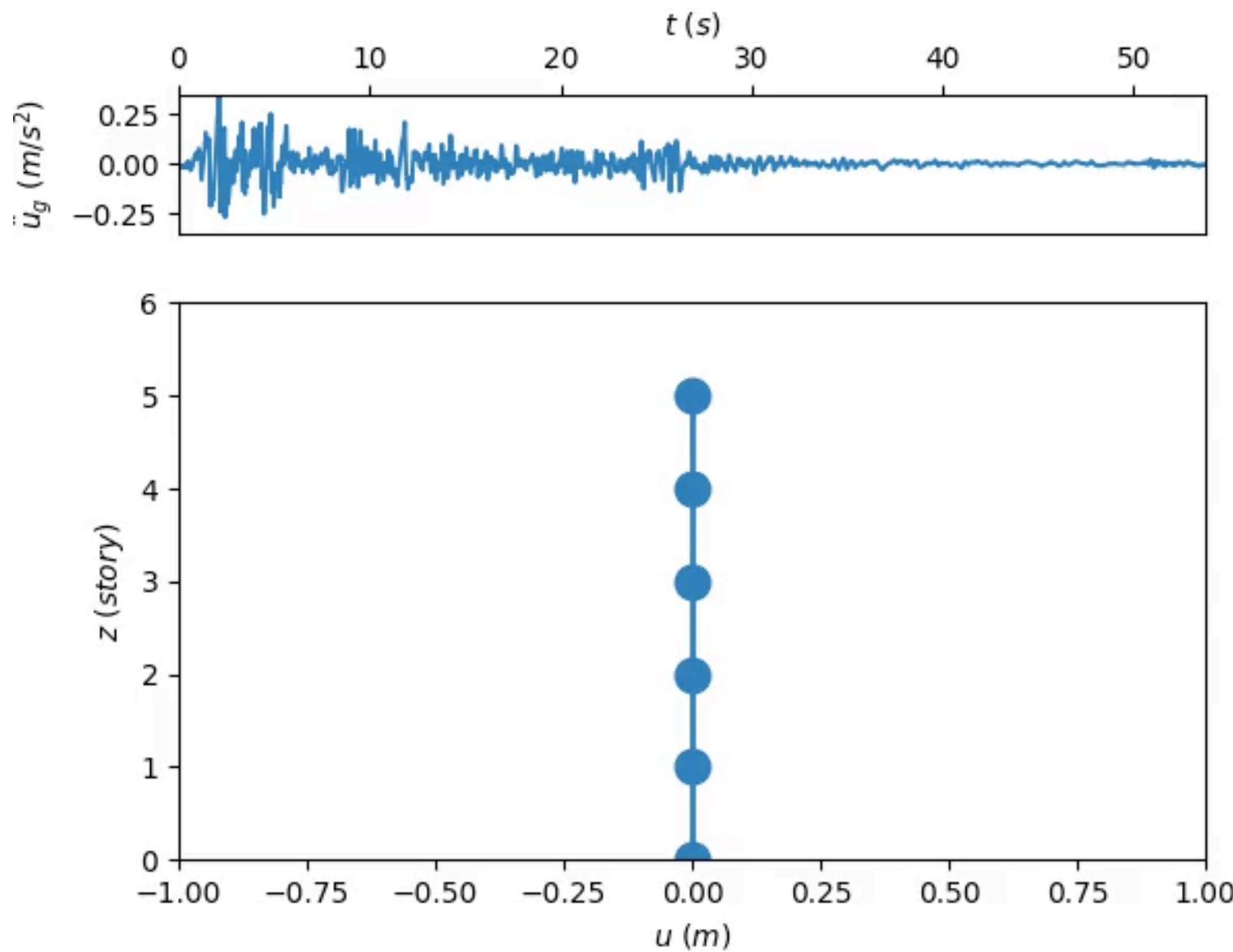
Local Nonlinear Search: Illustration



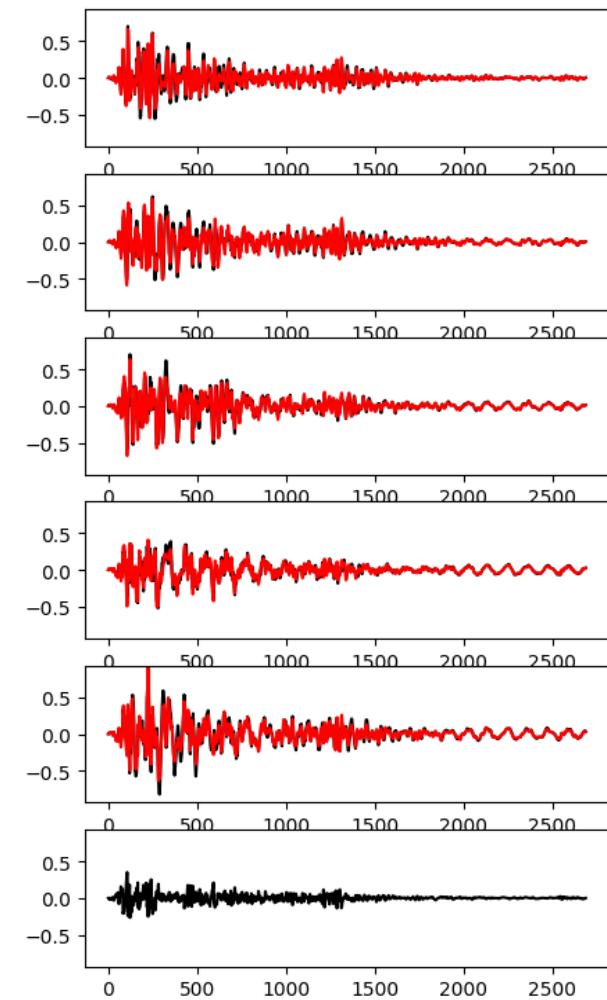
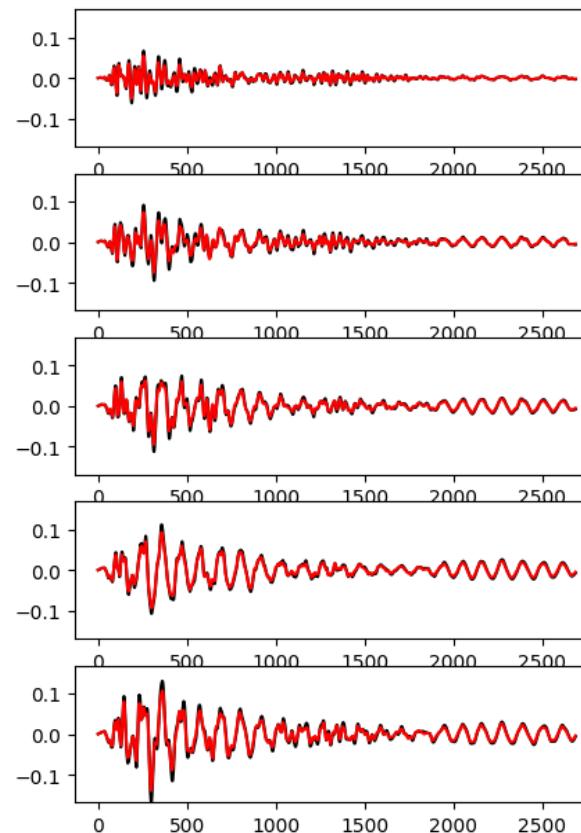
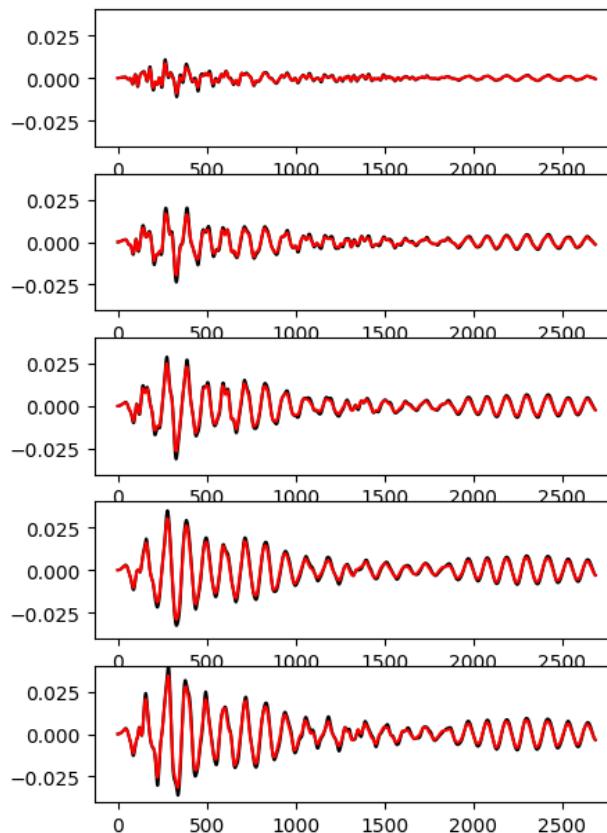
Local Nonlinear Search: Illustration



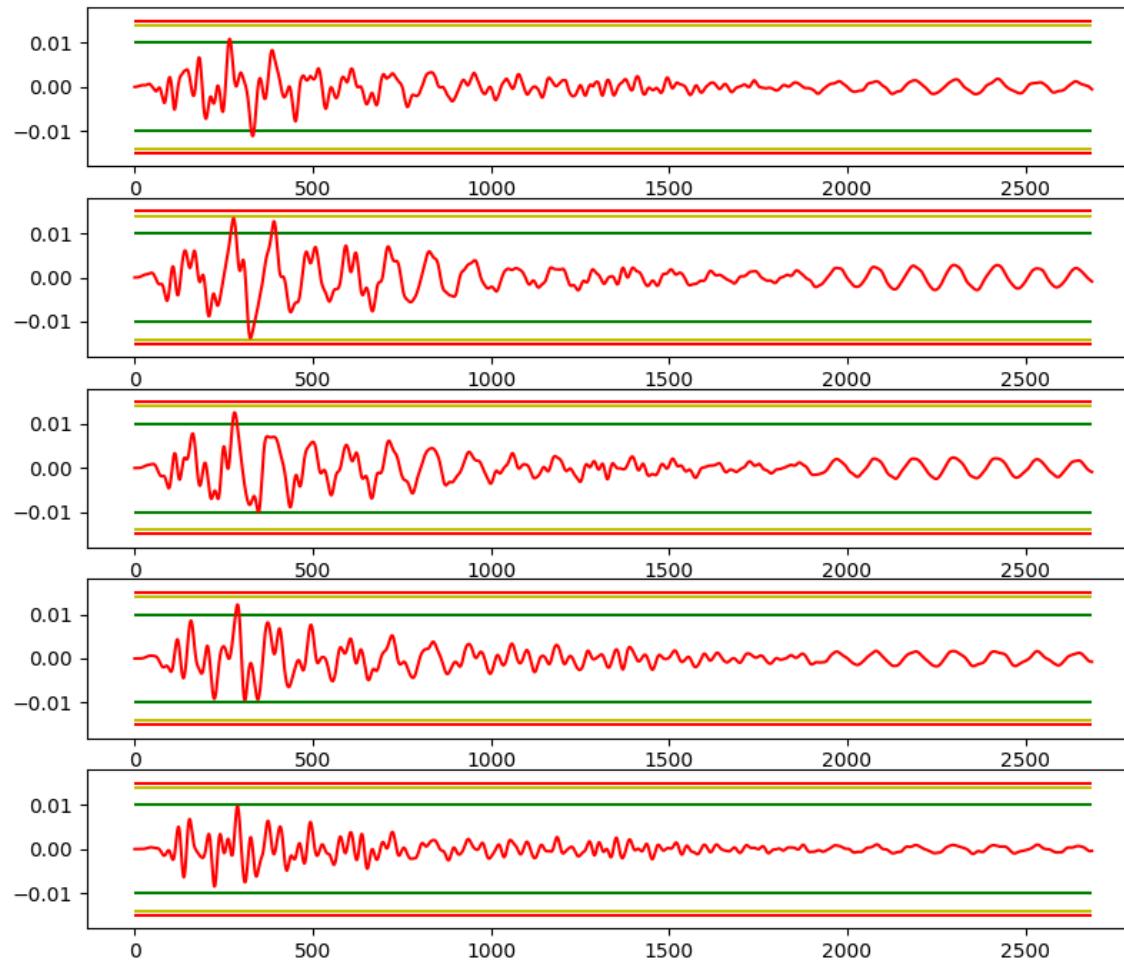
Example Dynamics



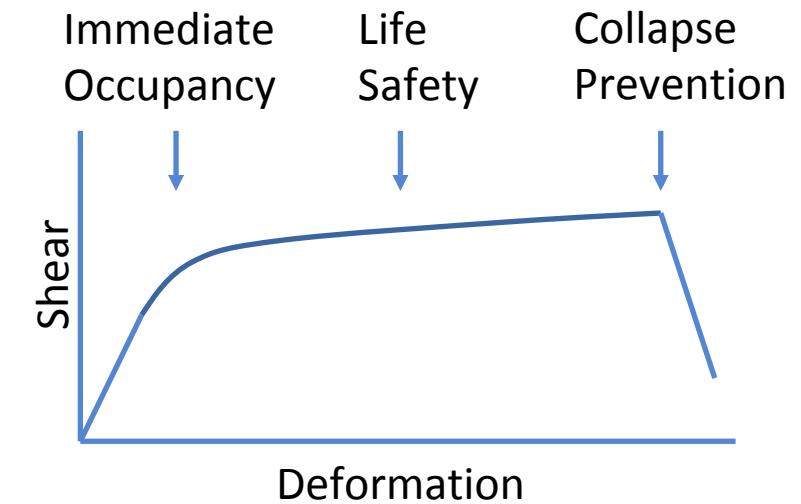
Dynamics and Predictions



Damage Estimation: Interstory Drift



Linear-Elastic
Range



Damage Estimation: Predictive Degradation

